

$GFR = \text{Glomerular filtration rate} = \frac{n \pi R^2 \Delta p}{8 \mu L}$

$R = 100 - 200 \text{ \AA}$

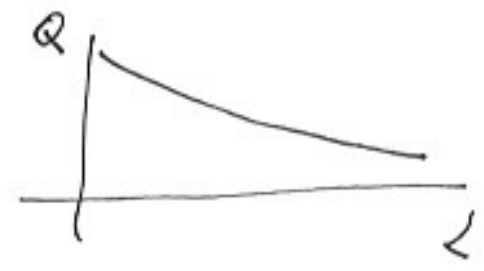
$L = 40 - 600 \text{ \AA}$

$GFR = 125 \frac{\text{ml}}{\text{min}}$

$\Delta p = 60 - 80 \text{ mmHg}$

$\mu = 4 \text{ Poise}$

$Q_{\text{Renal}} = 1200 \frac{\text{ml}}{\text{min}}$



$\overset{GFR}{dQ}$ 

$$\frac{dQ}{dx} = K \frac{S}{L} P_{UF}$$

P_{UF} = pressione di ultrafiltrazione

$$P_{UF} = (P_C - P_B) - (\pi_C - \pi_B)$$

$$P_{UF} = \Delta p - \pi_c$$

$$\pi_c = a_1 C + a_2 C^2$$

$$-\frac{\dot{m}}{c^2} \frac{dc}{dx} = \frac{-KS}{L} [\Delta p - a_1 C - a_2 C^2]$$

$$\frac{dQ}{dx} = \frac{KS}{L} [\Delta p - a_1 C - a_2 C^2]$$

$$\frac{dc}{dx} = \frac{KS}{L \dot{m}} [\Delta p - a_1 C - a_2 C^2] C^2$$

$$C = \frac{\dot{m}}{Q} = \frac{kg}{s} \cdot \frac{s}{ml} = \frac{kg}{ml}$$

$$Q = \frac{\dot{m}}{C}$$

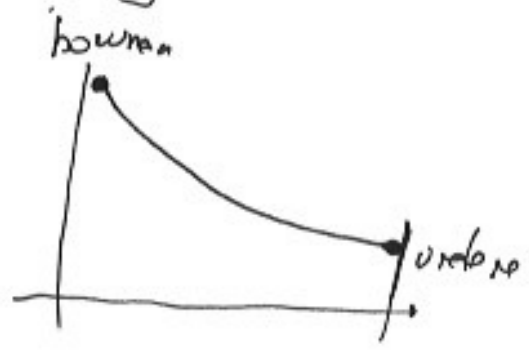


$C_{glucosio}$ (sangue)
 $C_{glucosio}$ (urine)

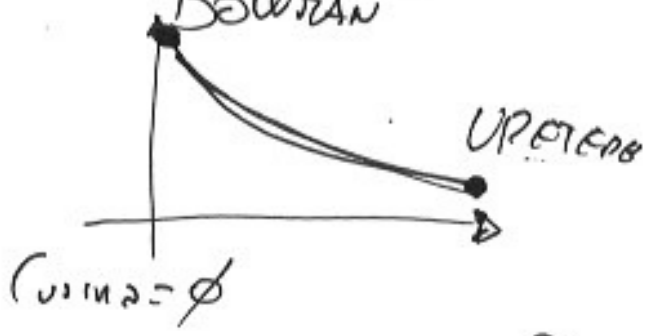
$$\frac{dQ}{dx} = \frac{d}{dx} \left(\frac{\dot{m}}{C} \right) = \dot{m} \frac{d}{dx} \left(\frac{1}{C} \right) = -\frac{\dot{m}}{C^2} \frac{dc}{dx}$$

$$\frac{dc}{dx} = -\frac{KS}{\Delta m} [\Delta p - a_1 C + a_2 C^2] C^2$$

$C_{glucosio}(\text{urine})$
 $C_{glucosio}(\text{sangue})$



$C_{blood} - C_{urina} = \Delta C \Rightarrow$ membrana basale BOWMAN



Urea = $\Delta C = \phi$
 Proteine = $\Delta C = C_{blood}$
 Sali = $\Delta C =$
 Na^+



$pH \text{ Sangue} = pH \text{ ULTRAFILTRATO}$

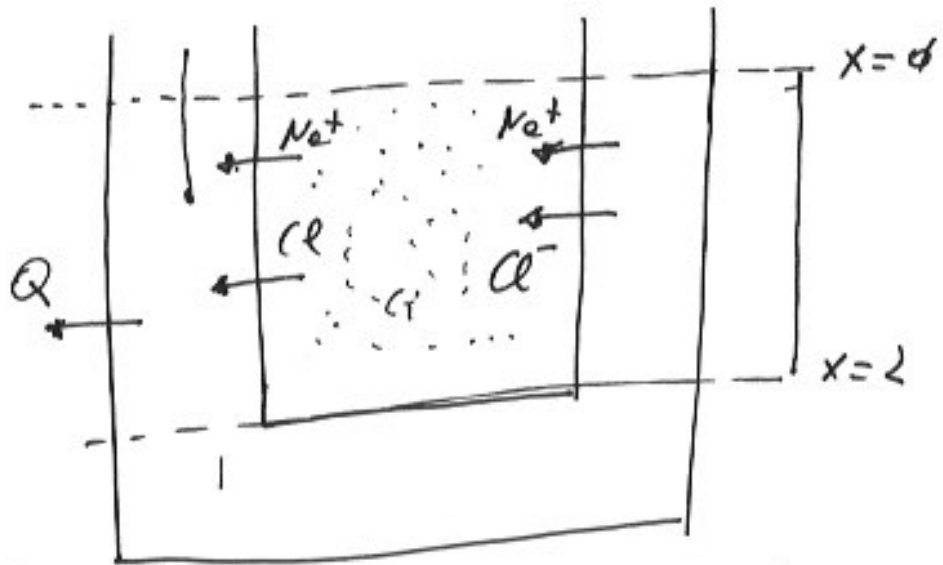
urina $\xrightarrow{PH \text{ Acido}}$ $\xrightarrow{PH \text{ basico}}$ $\xrightarrow{\text{Produzione di } CO_2}$ $\xrightarrow{\text{Tessuti oss.}}$
 PH BASICO $\xrightarrow{PH \text{ acido}}$ $\xrightarrow{\text{Eroci si}}$ $\xrightarrow{\text{NECROSI}}$

| PROSSIMITÀ | TIENDE | DISTANZA | COLLETTORE |

$$\frac{d(Q_{w,j} C_{ij})}{dx_j} = -2\pi R_j n J_{ij}$$

$$\frac{d(Q_{w,j} C_{i,j})}{dx_j} = -2\pi \underline{R_j} \underline{n} \cdot \underline{J_{ij}}$$

$$\begin{aligned}
 J_w &= k_w Q_w x \\
 J_{Na} &= \frac{k_{Na} [C_{Na,i} - C_{Na,o}]}{L} \\
 J_{Ne} &= k_{Na} C_{Na,i} \cdot l
 \end{aligned}$$



L = 1 cm

$$- \frac{d(Qc_d)}{dx} = K_d (c_d - c_i) \quad (1)$$

c_d = concentrazione Sodio nel tratto discendente

$$Q_a \frac{dc_a}{dx} = K_a (c_a - c_i) \quad (2)$$

c_a = concentrazione Sodio nel tratto ascendente

$$- \frac{dQ}{dx} = K_o (c_i - c_d) \quad (3)$$

c_i = concentrazione Sodio nell'interstizio

$$K_o c_a = -K_d (c_d - c_i) \quad (4)$$

(2)

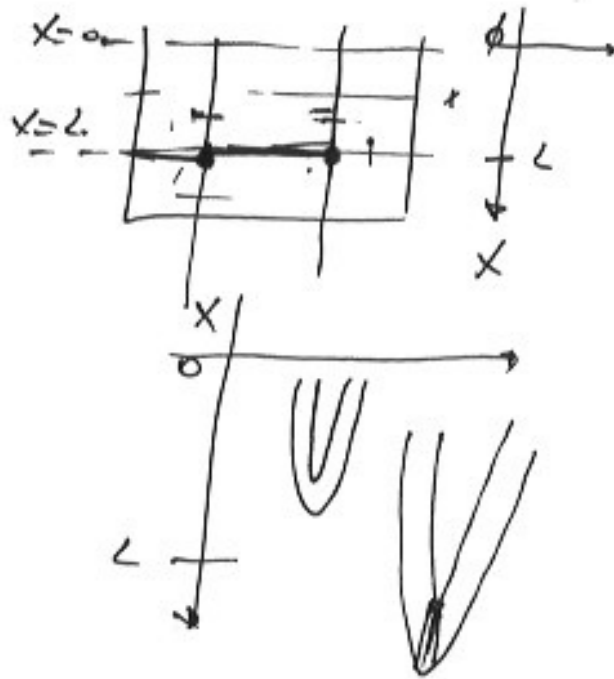
$$Q_a \frac{dC_a}{dx} = K_a C_a$$

$$\frac{dC_a}{C_a} = \frac{K_a}{Q_a} dx$$

$$\int_{C_a(0)}^{C_a(x)} \frac{dC_a}{C_a} = \int_0^x \frac{K_a}{Q_a} dx$$

$$\ln \frac{C_a(x)}{C_a(0)} = \frac{K_a}{Q_a} x$$

$$\frac{C_a(x)}{C_a(0)} = e^{\frac{K_a}{Q_a} x}$$



$$C_a(x) = C_a(0) e^{\frac{K_a}{Q_a} x}$$

(6)

$$-\frac{dQ}{dx} = K_0 (C_i - C_d)$$

$$K_a C_a = -K_d (C_d - C_i) = K_d (C_i - C_d)$$

$$(C_i - C_d) = \frac{K_a C_a}{K_d}$$

$$-\frac{dQ}{dx} = \frac{K_0 K_a}{K_d} C_a$$

$$-Q(x) + Q(0) = \frac{K_0 K_a}{K_d} (a(0) \cdot \frac{Q_0}{K_a} \cdot e^{\frac{K_0}{Q_0} x} \Big|_0^x$$

$$-\int_{Q(0)}^{Q(x)} dQ = \frac{K_0 K_a}{K_d} \int_0^x C_a dx$$

$$-Q(x) + Q(0) = \frac{K_0 K_a}{K_d} (a(0) \frac{Q_0}{K_a} [e^{\frac{K_0}{Q_0} x} - 1])$$

$$Q(x) = Q(0) - \frac{K_0}{K_d} (a(0) \frac{Q_0}{K_a} [e^{\frac{K_0}{Q_0} x} - 1])$$

$$-Q(x) + Q(0) = \frac{K_0 K_a}{K_d} \int_0^x C_a dx$$

8

$$- \frac{d(Qd)}{dx} = k_d (c_d - c_i)$$

$$K_a c_a = -k_d (c_d - c_i)$$

$$+ \frac{d(Qd)}{dx} = +K_a c_a$$

$$d(Qd) = K_a c_a dx$$

$$\int_{Q(0)c_d(0)}^{Q(x)c_d(x)} d(Qd) = K_a \int_0^x c_a dx$$

$$Q(x)c_d(x) - Q(0)c_d(0) = K_a \int_0^x c_{a0} e^{\frac{k_d}{D} x} dx$$

$$Q(x)c_d(x) - Q(0)c_d(0) = \frac{K_a Q_a}{K_a} c_{a0} \left[e^{\frac{k_d}{D} x} - 1 \right]$$

$$c_d(x) = \frac{Q(0)c_d(0) + K_a c_{a0} \left[e^{\frac{k_d}{D} x} - 1 \right]}{Q(x)}$$

9

$$C_d(x) = \frac{Q(0) C_d(0) + Q_a (a_0 [e^{\frac{k_a}{Q_a} x} - 1])}{Q(0) - \frac{k_0}{k_d} (a_0 Q_a [e^{\frac{k_a}{Q_a} x} - 1])}$$

$$C_a(x) = (a_0) e^{\frac{k_a}{Q_a} x}$$

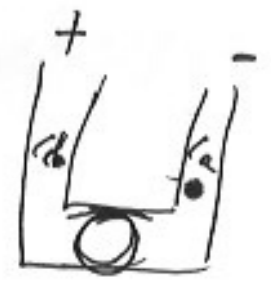
$$Q(x) = Q(0) - \frac{k_0}{k_d} (a_0 Q_a [e^{\frac{k_a}{Q_a} x} - 1])$$

$$k_a C_a = -k_d (C_d - C_i)$$

$$C_i = \phi \quad \frac{k_a C_a = -k_d C_d}{\text{fisiologica}}$$

$$C_i = \phi \quad C_a \gg C_d \quad \text{fisiologica}$$

$$C_i = \phi \quad C_a \ll C_d \quad \text{calcolosi - patologica}$$

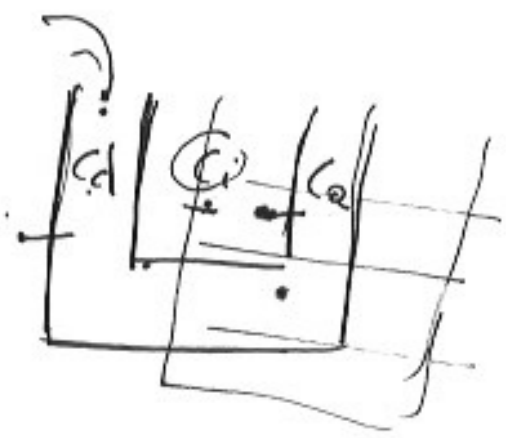


$C_i \neq 0$	$C_i = C_a = C_d$
--------------	-------------------

$C_i \neq 0$ $C_i \ll C_d$ $C_i \ll C_a$.
 patologica
sclerotizzazione renale.

$C_i \neq 0$ $C_i \ll C_d$ $C_i \gg C_e$.
 fisiologica → dieta iposodica.

$C_i \neq 0$ $C_i \gg C_d$ $C_i \gg C_a$.
 patologica
edema renale → ritenzione idrica.



$C_i \neq 0$ $C_i \gg C_d$ $C_i \ll C_a$.
 fisiologica. → dieta ricca in sal.

Cloro

(11)

$$\left\{ \begin{aligned} - \frac{d(Qc_d)}{dx} &= K_d (c_d - c_i) \end{aligned} \right.$$

C_a = Concentrazione Cloro
nel tratto ascendente

$$Q_a \frac{dC_a}{dx} = K_a (C_a - C_i)$$

C_d = concentrazione Cloro
nel tratto discendente

$$- \frac{dQ}{dx} = k_o (C_i - C_d)$$

C_i = concentrazione del Cloro
nell'interstizio

$$K_a (C_a - C_i) = -K_d (C_d - C_i)$$

$$C_i - C_d = C^*$$

$$\left\{ \begin{aligned} - \frac{d(Qc_d)}{dx} &= -K_d C^* \quad (1) \end{aligned} \right.$$

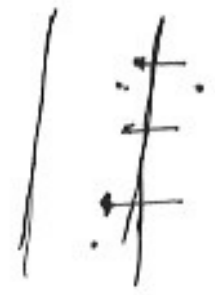
$$Q_a \frac{dC_a}{dx} = K_a (C_a - C_i) \quad (2)$$

$$- \frac{dQ}{dx} = K_o C^* \quad (3)$$

$$K_a (C_a - C_i) = +K_d C^* \quad (4)$$

③

$$-\frac{dQ}{dx} = K_0 C^*$$



$$-\frac{dQ}{dx} = K_0 C^* dx$$

$$-\int_{Q(0)}^{Q(x)} dQ = K_0 \int_0^x C^* dx$$

$C^* = \text{const}$

$$-Q(x) + Q(0) = K_0 C^* x$$

$$Q(x) = Q(0) - K_0 C^* x$$

125 ml/m

$$- \frac{d(Qc_d)}{dx} = -k_d c^*$$

$$+ Q \frac{dc_d}{dx} + c_d \frac{dQ}{dx} = +k_d c^*$$

$$\therefore \frac{dQ}{dx} = k_0 c^*$$

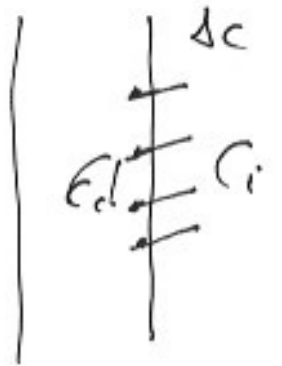
$$Q \frac{dc_d}{dx} + c_d (-k_0 c^*) = k_d c^*$$

$$Q \frac{dc_d}{dx} = k_d c^* + k_0 c^* c_d = c^* [k_d + k_0 c_d]$$

$$\frac{dc_d}{k_d + k_0 c_d} = \frac{c^*}{Q} dx = \frac{c^*}{Q(0) - k_0 c^* x} dx$$

$$\ln \frac{k_d + k_0 C_d(x)}{k_d + k_0 C_d(0)} = - \ln \left[\frac{Q(0)}{C^*} - k_0 x \right] \cdot \frac{C^*}{Q_0}$$

$$\ln \frac{k_d + k_0 C_d(x)}{k_d + k_0 C_d(0)} = - \ln \left[\frac{(Q(0) - k_0 x C^*)}{C^* Q_0} \right]$$



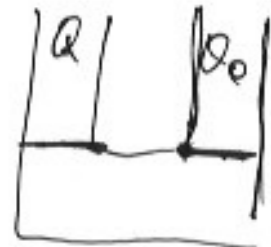
$$\frac{k_d + k_0 C_d(x)}{k_d + k_0 C_d(0)} = \frac{C^* Q_0}{C^* [Q(0) - k_0 x C^*]}$$

$$k_d + k_0 C_d(x) = \frac{[k_d + k_0 C_d(0)] [C^* Q_0]}{C^* [Q(0) - k_0 x C^*]}$$

$$C_d(x) = \frac{[k_d + k_0 C_d(0)] [C^* Q_0]}{k_0 C^* [Q(0) - k_0 x C^*]} - \frac{k_d}{k_0}$$

$$Q_a \frac{dC_a}{dx} = K_a (C_a - C_i)$$

$$K_a (C_a - C_i) = K_d C^*$$



$$Q_a \frac{dC_a}{dx} = K_d C^*$$

$$Q_a dC_a = K_d C^* dx \quad Q_a = Q(L)$$

$$dC_a = \frac{K_d}{Q_a} C^* dx$$

$$\int_{C_a(0)}^{C_a(x)} dC_a = \frac{K_d}{Q_a} C^* \int_0^x dx$$

$$C_a(x) - C_a(0) = \frac{K_d}{Q_a} C^* x$$

$$\boxed{C_a(x) = C_a(0) + \frac{Q_0}{Q_a} C^* x}$$

C_a C_i C^{*} C_{loro}

C_i = φ C^{*} = - E_d C_a C_i = φ

K_a C_a = - K_d C_d C_a ≠ C_d



C_i = φ C_a >> C_d patologica edema renale

C_i = φ C_a << C_d patologica sangue basificando

C_i = φ C_a = C_d fisiologica

C_i ≠ φ fisiologica C_i = 0

C_i ≠ φ patologica dialisi